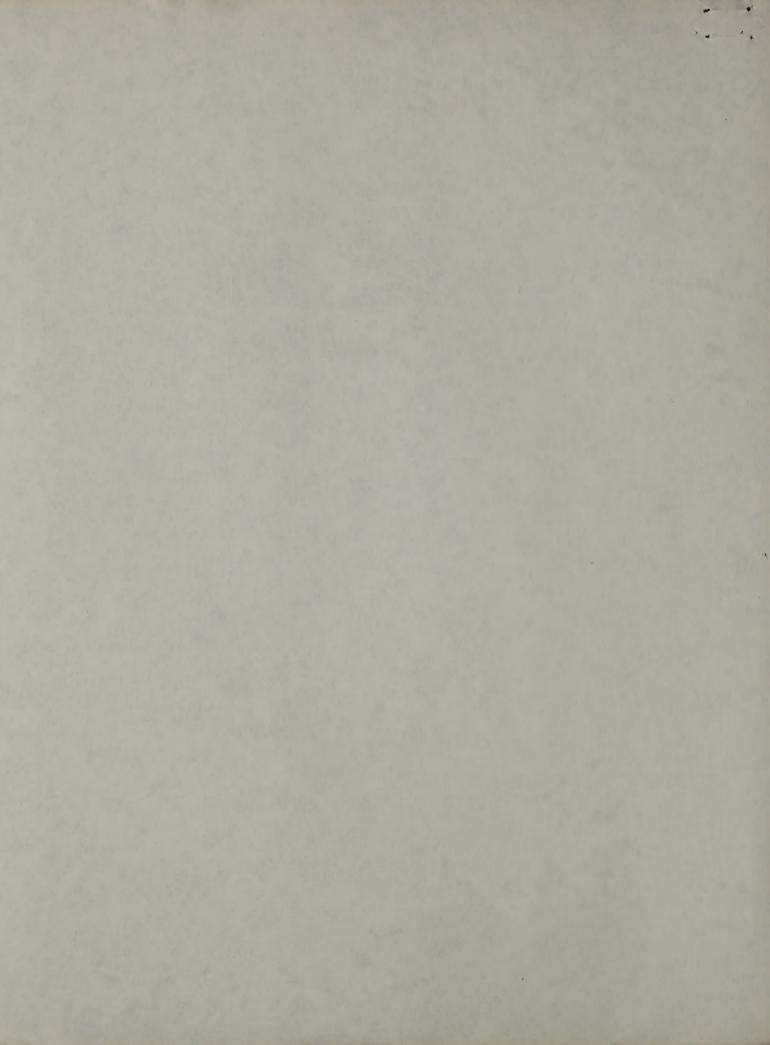
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THE ROLE OF THE WAVE EQUATION IN RATIONAL DESIGN OF PILE FOUNDATIONS

by

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New York State Department of Transportation
Soil Mechanics Bureau

November, 1976



NEW YORK STATE DEPARTMENT OF TRANSPORTATION SOIL MECHANICS BUREAU

"THE ROLE OF THE WAVE EQUATION
IN RATIONAL DESIGN OF PILE FOUNDATION"

RATIONAL PILE FOUNDATION DESIGN PROCEDURE

I. SUBSURFACE CONDITIONS DETERMINATION

- 1. Perform subsurface explorations and construct a soil profile including layer boundaries and possible obstructions, man-made or natural.
- 2. Assign engineering parameters to each soil layer using all available subsurface information, after completion of a testing program. (Friction angle, cohesion, density, etc.)
- 3. Identify and classify zones in the soil profile according to whether they are favorable or unfavorable with respect to foundation performance, i.e. a) Favorable: Strong, relatively incompressible, b) Unfavorable: Weak, compressible.

II. LOAD ANALYSIS

Determine the nature and magnitude of the loads to be supported and the probability of their occurrence to facilitate the selection of a foundation design.

III. ALTERNATE DESIGNS

At this point, reconsider all other foundation types and treatments which would provide a viable alternate to a pile foundation.

IV. FRICTION PILE ANALYSIS

1. A qualitative analysis of potentially suitable pile types is made by successively evaluating support capacity in each of the favorable zones of the subsurface profile. Include an evaluation of detrimental effects of all overlying (Negative Skin Friction) and underlying (settlement) unfavorable zones. Eliminate all obviously unsatisfactory

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alternatives. For each appropriate pile type choose a diameter and reasonable load per pile and calculate a pile length using a static analysis. Determine if this pile length and type satisfies the design requirements for deflection and moment under the applied lateral load. (See Appendix A)

- 2. Estimate the installation problems to be encountered for each particular pile type, i.e. vibration, damage to existing structures, noise pollution requirements, pile heave, jetting, corrosion, discontinuities, etc., and eliminate unsuitable alternatives.
- 3. Make an economic comparison of remaining suitable alternatives using a cost per pile or a cost per ton-ft. of piles as the economic factor. Choose final designs.
- 4. Determine if pile load tests (Static, Constant Rate of Penetration, or Dynamic) are needed. If so include the procedure in the contract documents and decide whether to drive the test pile to a resistance or an elevation.
- 5. Establish necessary restrictions on installation; Tolerance requirements, jetting limitations, limitations on the use of spuds or followers. Include a generalized soil profile including relevant test data (See Figure 1) and all pertinent special notes to alert the Contractor of unusual foundation conditions or special requirements. (See Appendix B)

V. END BEARING PILES

In the event rock or a suitable dense layer is shallow enough to reach economically, End Bearing Piles should be considered for use. The design pile load is then established based on the bearing capacity of the dense soil or rock, the structural capacity of the pile and lateral load requirements.

VI. DESIGN REVIEW

A foundation engineer (preferably the engineer involved) should review the contract proposal and plans to determine if the contract documents are clear as to what the Contractor must do. BERNALDS : TOTAL SECRETARY OF SERVICE STATE OF SECRETARY SERVICES

VII. CONSTRUCTION CONTROL

After a project has been let for construction the Contractor must submit details of the pile driving equipment he intends on using (See Figure 2). We then either accept or reject this equipment based on wave equation analyses which test the capability of the equipment to drive the designated pile to the estimated length without damage. If the driving system is adequate, we then will specify the required blow count and other pertinent data to the Contractor.

VIII. APPLICATION OF STATIC ANALYSIS AND WAVE EQUATION ANALYSIS FOR CONSTRUCTION CONTROL

Wave equation analyses for construction control are generally begun on receipt of a Pile and Driving Equipment Data form (See Figure 2). This form is completed by the Contractor and submitted to the State at least 2 weeks prior to starting pile driving. This information is combined with previously determined soil properties and static analyses to perform wave equation analyses.

A. Typical Wave Equation Analysis for a Friction Pile

Our most common usage of the wave equation analysis is to determine driving criteria for friction piles. The output from this analysis is compared with actual field results to determine if the design capacity is being attained at the estimated length. If the actual blow count is less than the predicted, an immediate review must be made of all facets of the design to determine cause. Commonly encountered problems involve underestimating temporary remolding of the subsoil or only analyzing the initial pile driven when the design has included the effect of densification due to pile group installation.

Figures 3A, B, and C-1 through C-8 illustrate a simple typical friction pile analysis and wave equation input and output. The bearing graph shown in Figure 3C-8 is of most interest to field personnel because of the obvious relationships between capacity, stroke, blow count, and stress.

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B. Typical Wave Equation Analysis for an End Bearing Pile

For many years little attention was paid to installation of end bearing piles other than obtaining the established blow count criteria for "refusal" or "practical refusal". This lack of knowledge regarding the destructive capability of the hammer-pile system led to many damaged piles which were unnecessarily overdriven.

Figures 4A, B, and C-l through C-8 illustrate a simple typical end bearing pile analysis. Note in Figure 4C-8 the rapid increase in stress with increasing stroke and blow count.

At the time of driving certain subsurface conditions may exist that will greatly influence the required blow count obtained from the wave equation. Additional static analyses will be required to provide proper input to the wave equation. Commonly encountered situations and methods of solution are described below.

A. Soils Subject to Remolding During Pile Driving

During pile driving certain types of soil, namely silts and clays, exhibit a temporary loss of strength. The following procedure should be used to account for this phenomenon and the resulting low pile blow counts. (Figure 5)

- 1. Perform static analysis as in Appendix A to determine the length required for design capacity.
- 2. Using this length and remolded soil strengths (see Refs. 11 and 12) recompute the soil resistance along the pile and the capacity.
- 3. Input the remolded resistance and capacity values into the wave equation to determine required pile blow count at time of driving.
- 4. If the amount of soil strength regain (set-up) is in question, a retap of a previously driven pile should be made and the resulting blow count compared with wave equation results from the original static analysis and actual design capacity. The duration of time between driving and retap should be based on an analysis of the drainage properties of the soil.

B. Soils Subjected to Scour

The foundations for structures at water crossings must be designed to sustain extreme flooding which will cause erosion or scour at piers. Therefore, piles are designed to achieve the design load below the depth of scour. However, the pile blow count at the time of driving will reflect penetration of the soil within the zone of scour. (Figure 6)

- 1. Estimate depth of maximum anticipated scour. (See Ref. 13)
- 2. Perform static analysis to determine pile length for required design capacity assuming zero soil resistance to scour depth.
- 3. Using that pile length, recompute actual soil resistance and actual pile capacity by including soil resistance within scour zone.
- 4. Input actual soil resistance and actual pile capacity into wave equation to determine required pile blow count at the time of driving.

C. Unfavorable Soil Deposit

Pile foundations often must completely penetrate deposits of favorable soil (or recent fill) and unfavorable soil which overlie the bearing stratum. Although these overlying layers do not contribute soil resistance to the design pile capacity, this resistance must be considered at the time of pile driving unless preaugering is utilized. (Figure 7)

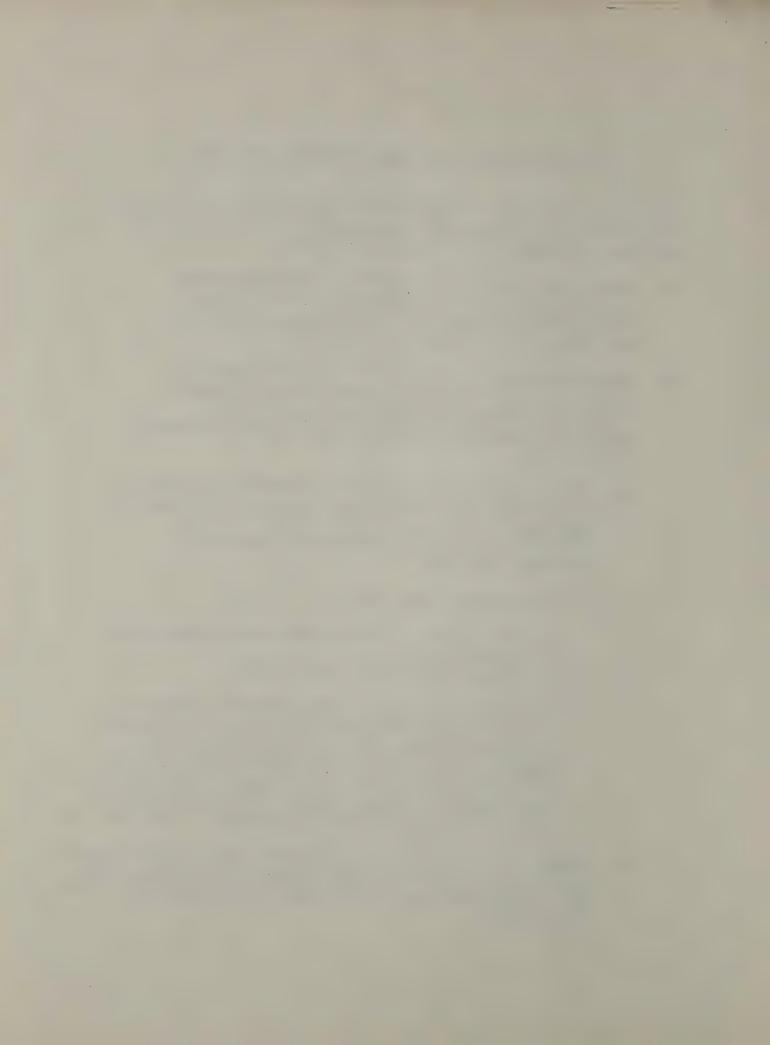
- 1. Perform static analysis to determine length of pile required in the proposed bearing stratum. Then determine total length.
- 2. Using that length recompute soil resistance including overlying soil layers and determine resulting capacity at time of pile driving.
- 3. Input the recomputed values into the wave equation to determine required blow count.



APPENDIX A

I. STATIC ANALYSIS FOR PILE BEARING CAPACITY

- A. Bearing Capacity of a Single Pile For each pile type under consideration a length will be determined, based upon the ultimate strength of the pile-soil system.
 - 1. Structural capacity of the Pile Determine the allowable load on the pile based on structural considerations alone, e.g. building code stresses. See Table 13-1 in Ref. #4 or Ref. #1.
 - 2. Bearing Capacity of the Soil A pile length is determined based on the ultimate shear strength of the soil using a safety factor of 2. The method of calculating the bearing capacity is based on soil type.
 - a. Cohesionless Soil (c=o) In granular materials two methods of analysis are used; for preliminary lengths use the approach as found in Broms (Ref. #2), for final lengths use Nordlund's Analysis (Ref. #8).
 - 1. Preliminary (Ref. #2)
 - a. End Bearing in TSF=2.5N(Stand. Penetration Resistance)
 - b. Skin Friction in TSF=.02 N
 - 2. Nordlund's Analysis This method is the best available for cohesionless soils. It accounts for more factors than any other equation. Densification of the soil due to pile driving, overburden reduction, pile volume, pile material, pile taper all these factors can be included in the calculation of bearing capacity. (See Ref. #8)
 - b. Cohesive Soils $(\emptyset=0)$ In cohesive soils a preliminary method is used based on the Standard Penetration Test and a more detailed method based on an empirical method by Tomlinson.



- Preliminary Undrained Shear Strength = N/8 (Ref. #2)
- 2. Tomlinson The adhesion of clay soils to piles is based on pile material and the strength of the clay. The stronger and stiffer the clay the more the adhesion is reduced relative to the shear strength of the soil (Ref. #10, Ref. #1 and Ref. #7). Also, in a layered system see Ref. #9., Tomlinson has taken into account the intrusion of upper layers carried into lower ones. Shear strength is based on a conservative interpretation of Laboratory and Field Testing Programs.
- 3. As a check, Broms Ref. #2 can be used to provide a range of results. These adhesion values are very conservative.
- c. Silty Soils (0 & c soils) Generally silts are analyzed similar to clays, using Tomlinson's analysis. However, the results should be checked with a drained analysis, (See Ref. #12, Chap. 21) assuming a drained friction angle.
- B. Bearing Capacity of Pile Groups This analysis is subdivided by soil type but in general the capacity of a pile group depends on the pile spacing.
 - 1. Cohesive Soils As per Ref. #7 the efficiency factor varies between 0.7 at a pile spacing of 3 pile diameters, to 1 at a spacing equal to 8 pile diameters. For spacings less than 3 the group fails as a block.
 - 2. Cohesionless Soils For sands and gravels and efficiency factor of 1 is a good design value as in Ref. #7.

II. SETTLEMENT

Settlement of a Pile Foundation - Settlement prediction is perhaps the least accurate of the aspects of pile design. For long term settlement of a pile group, the 2/3 rule method as outlined in NAVDOCKS Ref. #4 is used.

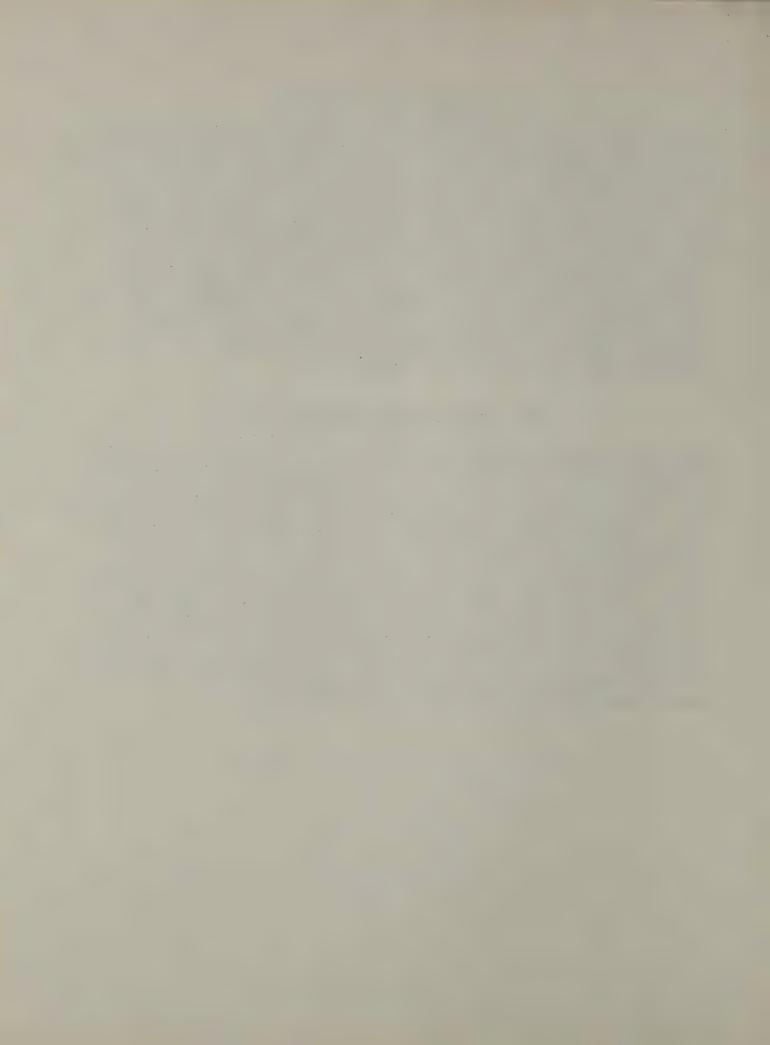


III. NEGATIVE SKIN FRICTION

Negative skin friction is caused by a relative downward movement of the soil surrounding a pile. All available downdrag or negative skin friction will be mobilized whenever there is more than 0.4" relative movement between pile and soil in cohesionless soils and 0.2" relative movement in cohesive soils. Therefore, whereever such movements can occur, negative skin friction should be accounted for. Please note that although Tomlinson's adhesion values are conservative when used in bearing capacity analyses, unconservative negative skin friction values will result unless the adhesion values are increased. At present NAVDOCK'S Ref. #4 gives the most general method for determining negative skin friction. However, for end bearing piles Garlanger (Ref. #6 and Fellenius (Ref. #5) are promising methods.

IV. LATERAL LOAD ANALYSIS

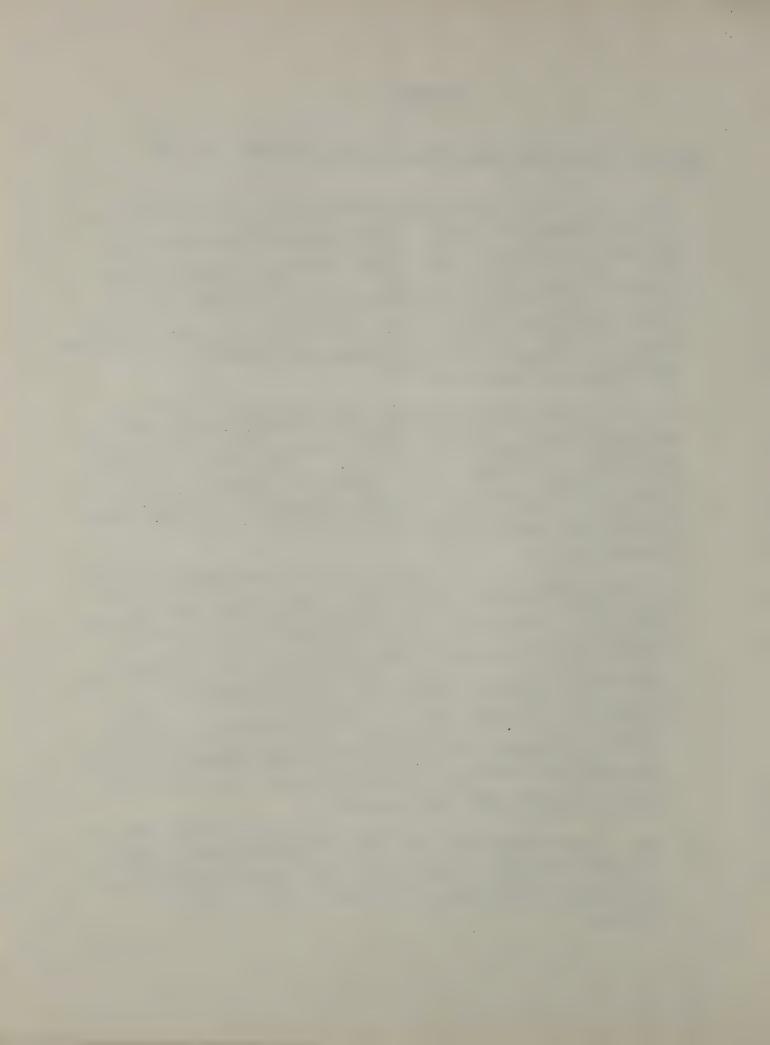
The relationships between applied lateral load, pile moment and deflection, and soil parameters are determined for a single pile by a method developed by Reese et al (References 14, 15, 16, 17). This method includes many pertinent design variables not accounted for in other methods, although a computer solution is required to incorporate all variables in the analysis. The computer program (code name COM 622) developed by Reese is available from the Computing Center, University of Colorado, Boulder, Colorado 80302. More general cases with no axial loads and constant pile stiffness may be readily solved by hand using non-dimensional coefficients in the aforementioned publication or by Broms (References 18, 19). As of now, no reliable method has been developed to ascertain pile group effects. The most promising method for groups was developed by Poulos (Reference 20).



APPENDIX B

TYPICAL SPECIAL CONTRACT NOTES FOR PILE DRIVING (NYS DOT)

- 1. "Piles will be acceptable only when driven to pile driving criteria established by the Deputy Chief Engineer (Structures). Prerequisite to establishing these criteria, the Contractor shall submit, to the Deputy Chief Engineer (Structures) and others as required, Form BD 138, 'Pile and Driving Equipment Data'. All information listed on Form BD 138 shall be provided within fourteen (14) days after the award of the contract. Each separate combination of pile and pile driving equipment proposed by the Contractor will require the submission of a corresponding Form BD 138."
- 2. "It is possible that difficult driving of piles may be encountered and it may be necessary to utilize mechanical equipment for removing consolidated material or boulders from the location of piles. This may be accomplished by various types of earth augers, well drilling equipment, or other devices to remove the consolidated material to permit piles to be driven to the desired depth or rated resistance without distortion."
- 3. "If any obstructions to pile driving are encountered ten (10) feet or less from the bottom of the footing, the Contractor shall, if so ordered by the Engineer, pull the partially driven pile or piles and remove the obstruction, backfilling the hole with approved suitable material which shall be thoroughly compacted to the satisfaction of the Engineer. However, no partially driven pile shall be removed until the Engineer is satisfied that the Contractor has made every effort to drive the pile through the obstruction. Payment for the excavation will be made at the unit price bid for the Structure Excavation Item and for the temporary sheeting under Item ______ when sheeting is used. No other extra payment will be made for this work."
- 4. "The ordered length of pile shall be measured below the cutoff elevation shown on the plans. Any additional lengths
 of pile or splices above the cut-off elevation necessary to
 facilitate the Contractor's operation shall be at his own
 expense."



- 5. "Piles for _____ are driven because of possible scour of stream bed and shall be driven to the minimum lengths shown on the plans regardless of the resistance to driving."
- on rock for the H-piles which will laterally support

 The hammer provided to drive these piles must be capable of achieving the required penetration through the compact overburden which may present hard driving conditions. To attain the necessary lateral resistance, these piles must penetrate to the ledge rock surface. Therefore, prior to pile driving approval of the Deputy Chief Engineer (Structures) will be required in accordance with Section 629 of the specifications. This approach shall be based on a review and evaluation of data submitted by the Contractor on Form BD 138."
- 7. "A static pile load test shall be performed at a location designated on the plans, or as specified by the Deputy Chief Engineer (Structures) in accordance with SCP-5 the Static Pile Load Test Manual. The pile load test shall consist of either the constant rate of penetration test or the maintained load test as specified. It shall be performed after a minimum seven (7) day waiting period. The Contractor shall prevent the test pile from rebounding during the waiting period and prior to application of the test loads.
- 8. "Dynamic load tests will be conducted by representatives of New York State on the Static Load Test Pile and at least one pile in each pier, or at other locations ordered by the Engineer. The Contractor shall furnish the appurtenant construction equipment necessary to perform the field tests in accordance with 'Furnishing Equipment for Dynamic Load Testing of Piles' Item."
- 9. "Piles for the existing structure should be removed where they interfere with the pile driving for the new structure."
- 10. "It shall be the Contractor's responsibility to place the cofferdams for _____ so that they will not interfere with the driving of batter piles. Pay lines for the cofferdams shall be as shown on the plans."
- 11. "The general subsurface conditions at the site of this structure are as shown on Drawing No. ____."



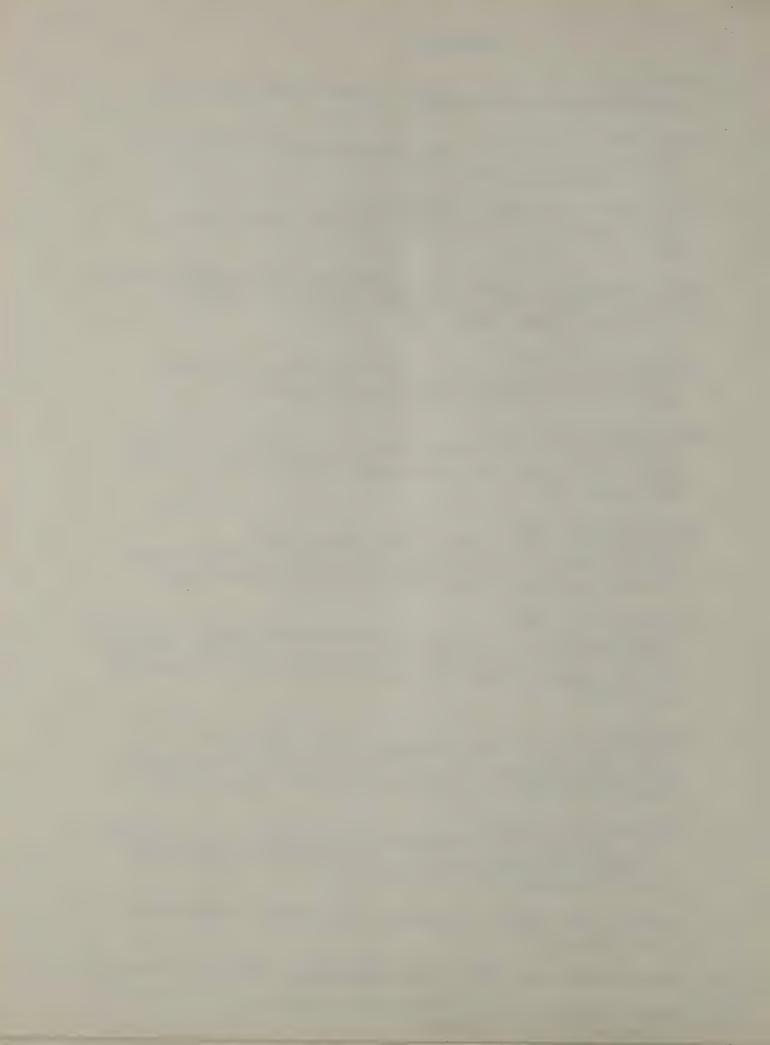
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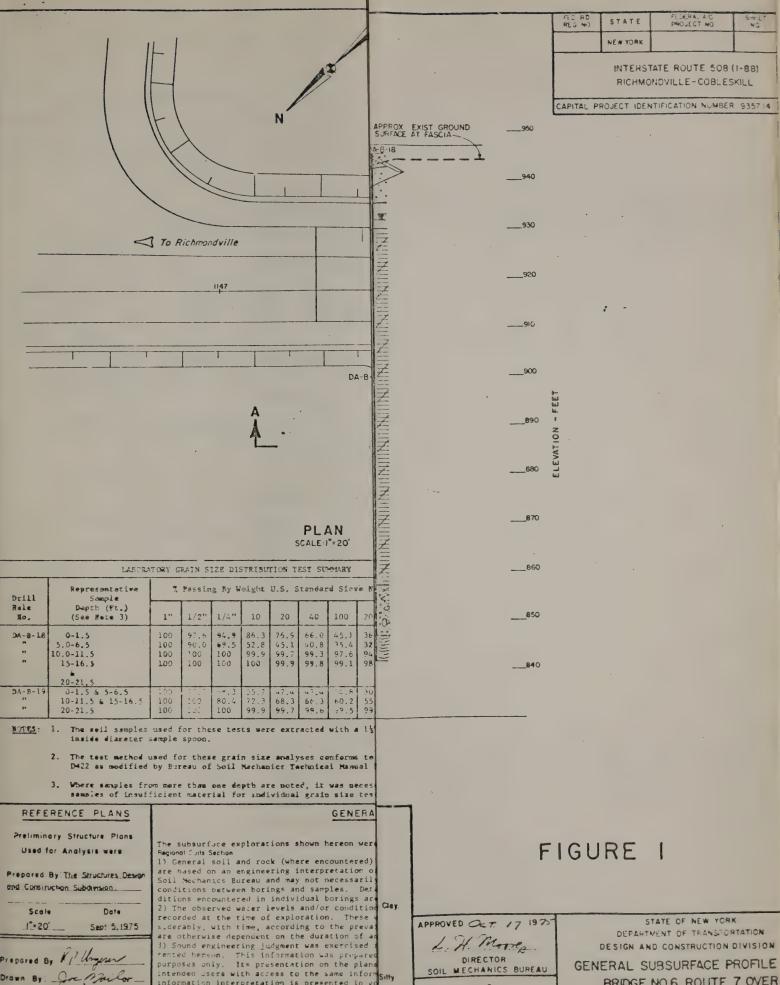
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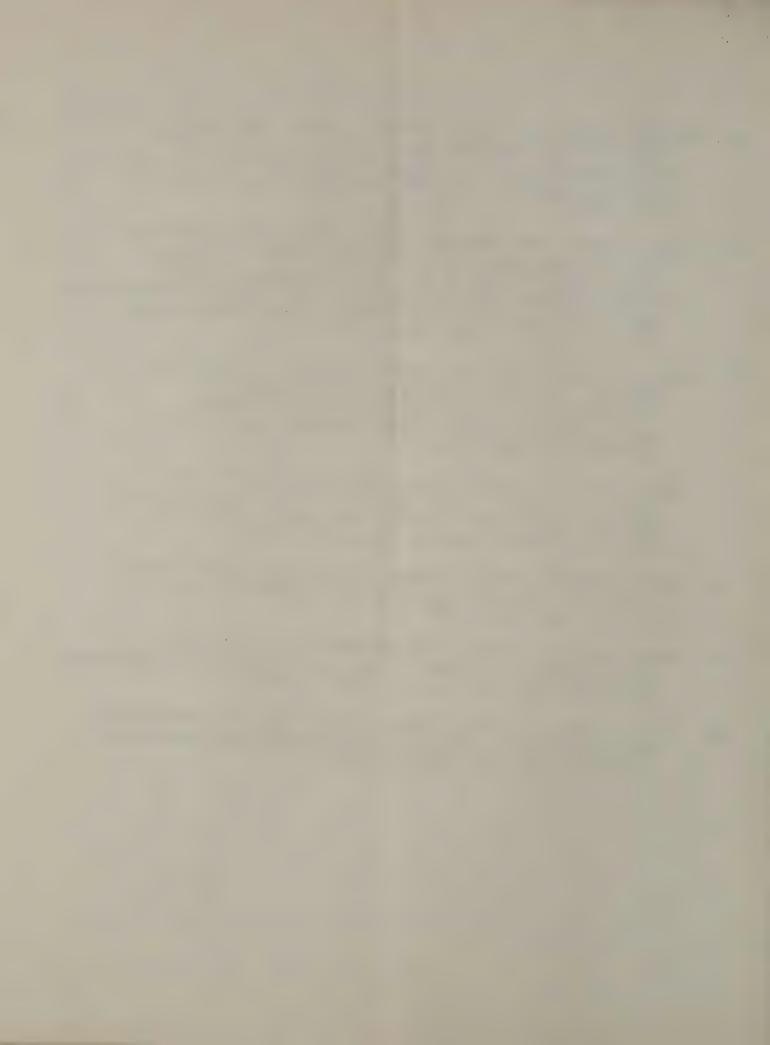


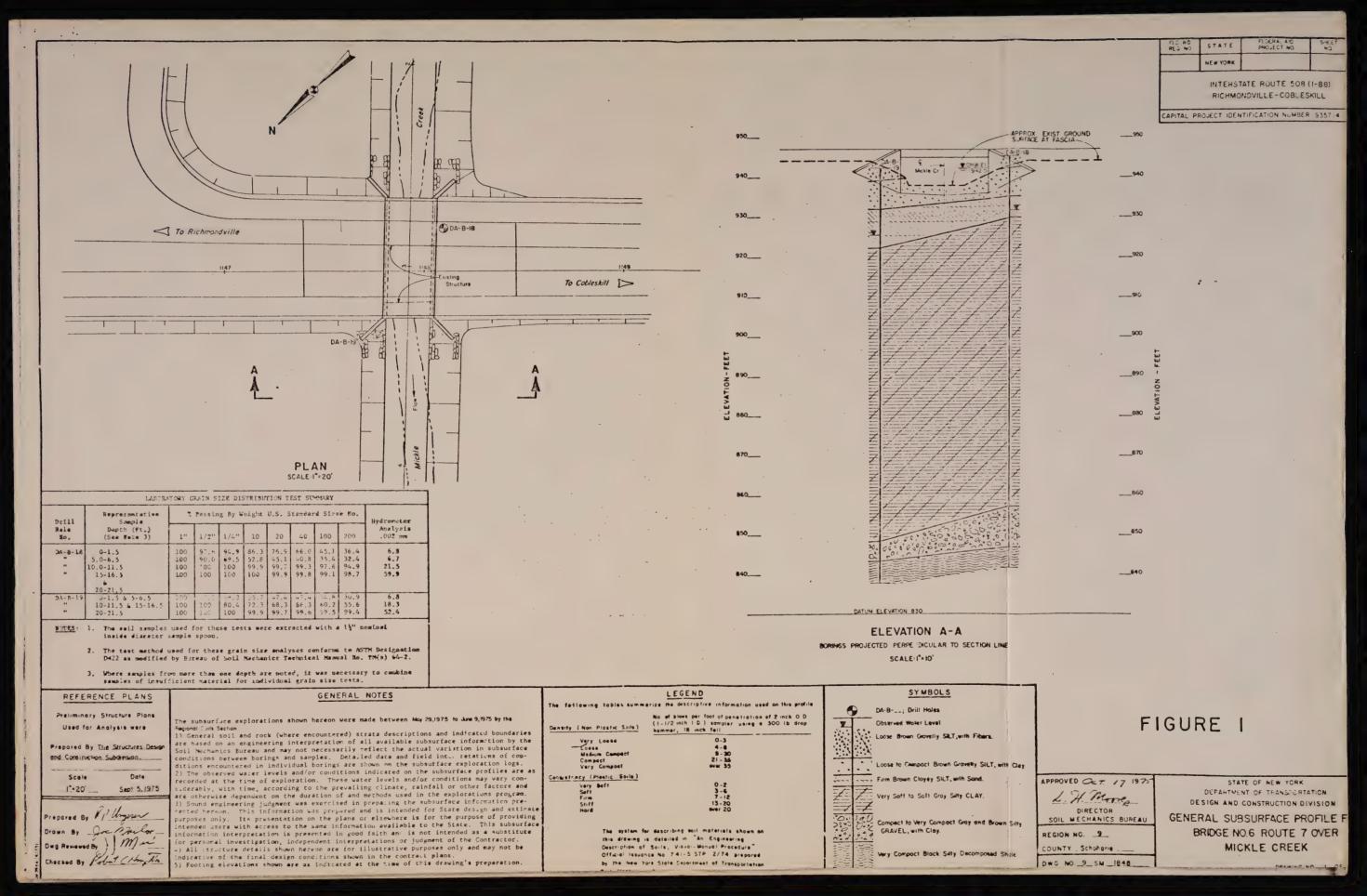
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intended users with access to the same inform Sitty information interpretation is presented in go information interpretation is presented in go for personal investigation, independent inter -) All itructure details shown hereon are for indicative of the final design conditions sho 5) Footing elevations shown are as indicated

REGION NG. 9

COUNTY Schoharia DWG NO 9_ SM _ 1848 GENERAL SUBSURFACE PROFILE F BRIDGE NO.6 ROUTE 7 OVER MICKLE CREEK



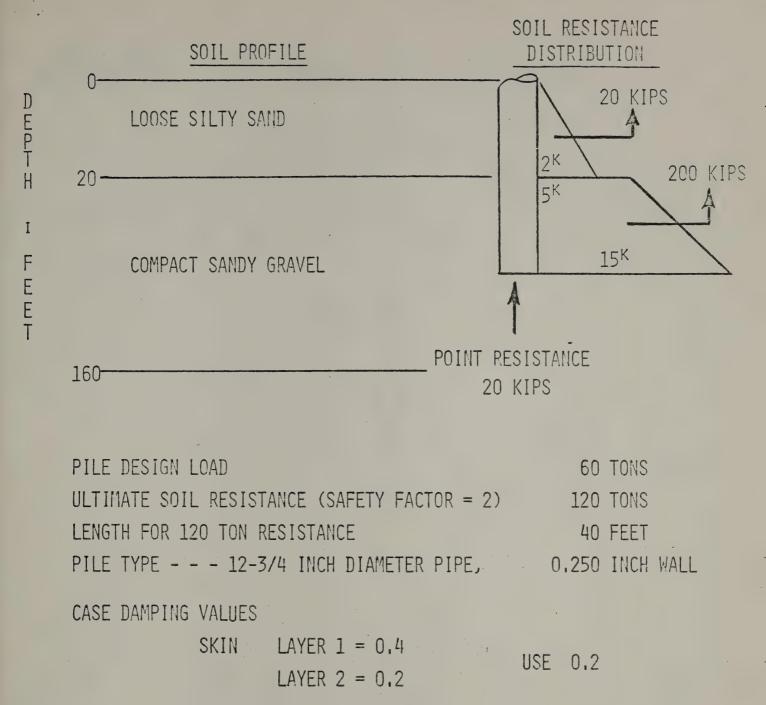




PILE AND DRIVING EQUIPMENT DATA

P. I. N.:(Structure Name	and/or No.:	
		,	•	tractor or Subc	ontractor:
County:			(Piles driven by)	
HAMMER COMPONENTS	HAMMER	Type: Rated Energy:	Seri	ol No.:	Length of Stroke
	RAM				diesel hammers)
	ANVIL				1
		Material:			Area
	CAPBLOCK	Modulus of Ela	sticity - E Restitution-e		(P. S.I.)
	PILE CAP	Helmet. Bonnet Anvil Block Drivehead	Weight:		
	CUSHION	Thickness: Modulus of Elas			Area:(R.S.L.)
	PILE	Pile Size: Les Dic Wall Thickness Material: Design Pile Cap		Taper:	
		NOTE: If mand manufac dimensi	relis used to dri turer's detail she	ve the pile, att	ach separate weight and





DESIGN DATA FOR WAVE EQUATION ANALYSIS

FRICTION PILE EXAMPLE

FIGURE 3A

0.1

0.1

0.1

TOE

TOE

QUAKE VALUES SKIN



INPUT CARD						
REFERENCE NO.	DESIGNATION OF NECESSARY INPUT					
	TITLE	TITLE				
1.0	FRICTION PILE					
	IOUT IHAMR IPERCS					
2.0	10, , 4, ,,,,,, 92 *					
	WT. CAP STIFF-CB					
3.0	1.2, 21,000., *					
	C.O.RCB					
4.0	, 0.8, *					
	LENGTH AREA-PILE TOP					
5.0	40.0, 9.8 , *					
	QUAKE-SKIN QUAKE-TOE DAMP-SKIN DAMP-TOE RULT					
6.0	0.1, 0.1, 0.2, 0.1, -1.0,	+				
•	X _{PI} % SOIL RESISTANCE					
6.401	0.0					
6.402	20.0					
6.403	20.0 5.0					
6.404	40.0					
7.0	BLANK					
8.0	BLANK					
	ULTIMATE RESISTANCE					
9.0	60.0, 90.0, 120.0 180.0, 240.0, *					
	CASE WAVE EQUATION INPUT					
	FRICTION PILE EXAMPLE					

FIGURE 3B



FRICTION PILE

PILE DESCRIPTION

```
X BEL. TOP (FT) 0.0 40.0
A (SQ. IN.) 9.8 9.8
E (KSI) 29000. 29000.
GAMMA (LB/CH FT) 492.0 492.0
```

	HAMMER MODE	EL DEL. nº	-22
ELEMENT	WEIGHT	STIFFNESS	COFFF.
NUMBER	(KIPS)	(K/IN)	RESTITUTION
1	1.213		
2	1.213	191666.7	
3	1.213	191666.7	
4 1	- 1.213	191666.7	
ANVIL	1.595	101833.3	0.850
CAP	1.200	21000.0	0.800
CUSHION		0.0	1.000
PILE THP	•		0.850

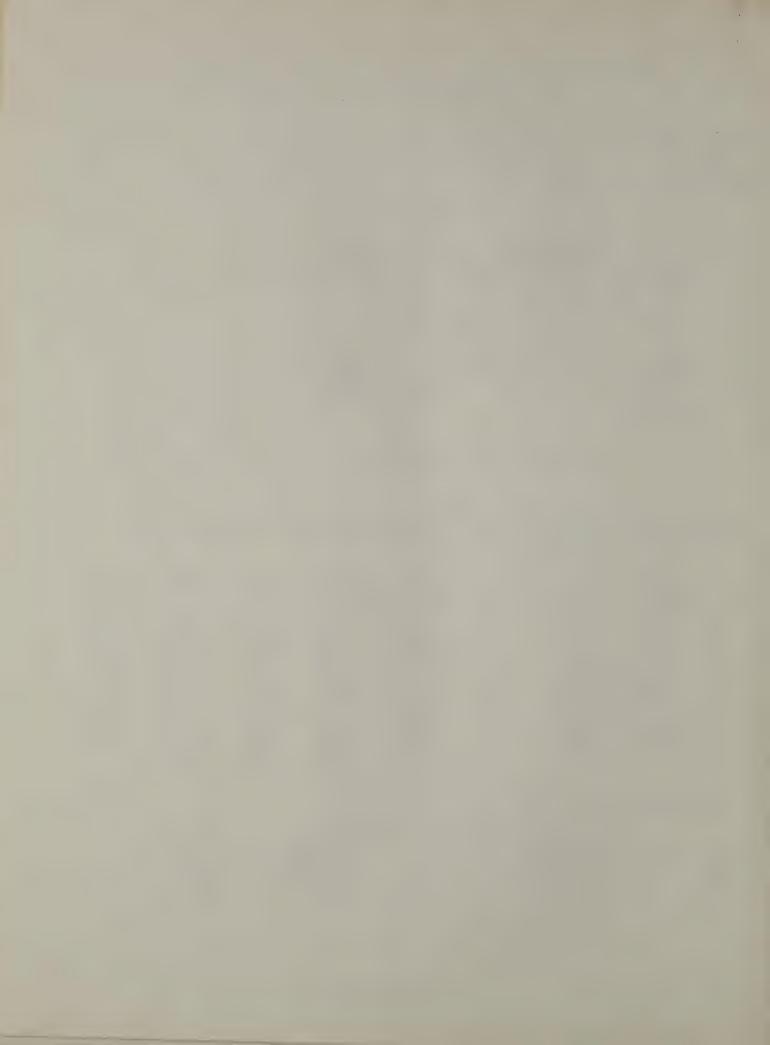
PILE PROPERTIES

PILE LENGTH= 40. FT., AREA(AT TOP)= 9.8 STIN E. MODUL(AT TOP)=29000. KSI., SPEC. WT.(AT TOP)= 492. LBS/CU FT

	WEIGHT		PDAMP.	SPLICE	-	.snIL=n	QUAKE	L.R.T.
NO.	(KIPS)	(KNIN)	(KS/FT)	(KIPS)	(PCT.)	(KS/FT)	(IN.)	(FT.)
1	0.149	5340.	0.34	. 0 •	0.004	0.015	0.100	4.4
2	0.149	5340.	0.34	-5000.	0.012	0.046	0.100	8.9
3	0.149	5340.	0.34	~ 5000•	0.021	0+077	0.100	13.3
4	0.149	5340.	0.34	- 5000•	0.029	0.108	0.100	17.8
5	0.149	5340.	0.34	~ 5000•	0.069	0.259	0.100	22.2
6	0.149	5340.	0.34	-5000 •	0.134	0.503	0.100	26.7
7	0 • 149	5340.	0.34	- 5000•	. 0.176	0.658	0.100	31.1
8	0.149	5340.	0.34	~ 5000∙	0.217	0.812	0.100	35.6
9	0.149	5340.	0.34	-5000 •	0.258	0.967	0.100	40.0
TOE					0.180	1.723	0.100	

COEFFICIENT OF RESTITUTION OF SOIL 1.000

		OPTIONS AND	SPECIFICAT	INNS	
PHI	1.40	S-DAMPING	VISCOUS	RWT (KIPS)	0.00
INUT	10	P-DAMPING	10 to	SOIL DIST. NO.	. 0
IFUEL	1	J SKIN	0.20	TDEL (SEC.)	0.0000
IOSTR	0	J TOE	0.10	TEMAX (MS)	0.00
		TIME INCR.	(MS)0.091	1	



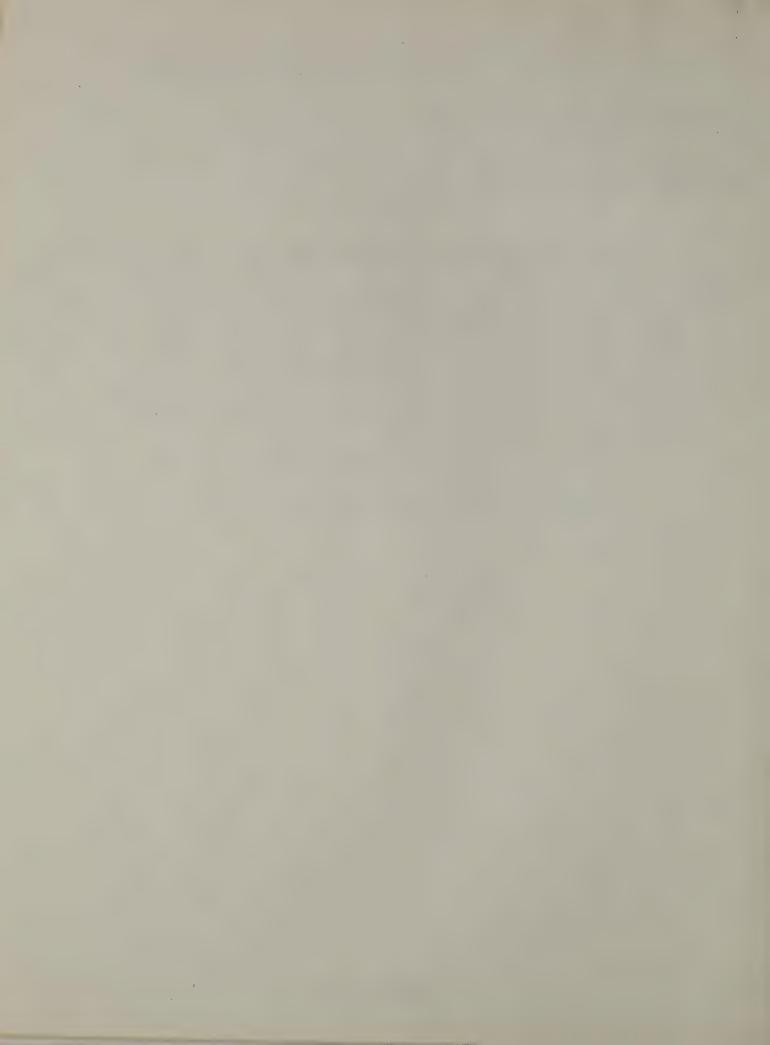
RULT= 60.0, AT TOE= 4.8 TONS

TRANSFERRED FNERGY, MAX= 27.7 K=FT FIN= 27.2 K=FT TRANSFERRED FNERGY, MAX= 21.1 K=FT FIN= 20.5 K=FT FIN= 22.4 K=FT FIN= 22.4 K=FT

	TABLE	OF EXTREME V	ALUES FOR PIL	E AND TIME	OF OCCURRENC	E
ELEM.	FMAX		MINSTR			DISHX
Nn.	KTPS	KIPS	KSI	KST	FT/S	INCH
1	269.2(71)	0.0(0)	0.0(-0)	27.4(71)	11.99(38)	1.824(289)
2	263.8(72)	0.0(0)	0.0(0)	26.9(72)	12.95(84)	1.804(290)
3	262.7(43)	0.0(0)	0.0(0)	26.3(43)	14.54(82)	1.783(290)
Ц	263.6(46)	0.0(0)	0.0(0)	26.8(46)	15.24(81)	1.763(293)
. 5	264.8(49)	0.0(0)	0.0(0)	27.0(49)	14.39(80)	1.744(300)
6	260.4(52)	0.0(0)	0.0(0)	26.5(52)	12.28(79)	1.727(301)
7	242.2(55)	0.0(0)	0.0(-0)	24.7(55)	11.92(94)	1.712(301)
8	203.7(57)	0.0(0)	0.0(0)	20.7(57)	13.45(97)	1.701(300)
9	132.4(58)	0.0(0)	0.0(0)	13.5(58)	15,86(64)	1.694(300)

THE MAXIMUM TRANSFERRED ENERGY (ENTHRU) WAS 22.9 K FT

STROKES ANALYZED AND LAST RETURN (FT) 5.0 3.7 4.0 3.9



RIII.T= 90.6, AT TOE= 7.2 TONS

TRANSFERRED FNERGY, MAY= 22.3 KTFT FIN= 20.6 KTFT

	TABLE	E OF EX	KTREME	VALUES F	OR PILE	AND .	TIME	ne accus	RENC	Ε
ELFH.	FMAX	F	MIN	MINS	TR	MAYS	TR	VELH	<	DISMX
Nn.	KIPS	7	CTPS	KS	Ţ	KS	T	FT/S	5	INCH
1	306.86 69	0.	0(0)	0.00	0)	31.20	69)	14.27(35)	1.354(214)
2	304.30 70	0.	0(0)	0.00	. 0)	31.00	70)	14.13(385	1.327(215)
3	299.66 39	0.	0(0)	0.00	0)	30.50	39)	14.320	79)	1.298(215)
4	300.3(43) 0.	0(0)	0.00	0)	30.50	43)	15.05(78)	1.269(217)
5	303.00 46	0.	0(0)	0.00	0)	30.90	46)	13.86(78)	1.241(219)
6	300.00 49) (n(0)	0.00	0)	30.50	49)	12.380	50)	1.215(219)
7	279.6(52	0.	n(0)	0.00	0)	28.50	52)	12.120	54)	1.192(217)
8	232.9(54	0.	0(0)	0.0(0)	23.7(54)	13.74(58)	1.175(218
9	149.8(56	0.	· n (0)	0.00	0)	15.30	56)	16.28(61)	1.164(220)

THE MAXIMUM TRANSFERRED EMERGY (ENTHRU) WAS 22.3 K-FT

STROKES ANALYZED AND LAST RETURN (FT) 4.8 4.6



RULT= 120.0, AT THE= . 9.6 THNS

TRANSFERRED ENERGY, MAX= 20.9 K=FT FIN= 18.1 K=FT

	TABLE	OF EXTREME	VALUES FOR PI	LE AND TIME	OF OCCURRENC	F
ELEM.	FMAX	FMIN	MINSTR	HAXSTR	VELMX	DISMY
NO.	KIPS	KTPS	KSJ	KST	FT/S	INCH
1	333.1(67)	0.0(0)	0.0(0)	33.9(67)	15.38(32)	1.075(164)
2	334.5(68)	0.0(0)	0.0(0)	34.1(68)	15.22(35)	1.037(165)
3	320.6(37)	0.0(0)	0.0(0)	32.6(37)	14.99(38)	0.997(166)
Д	321.4(40)	0.0(0)	0.0(0)	32.7(40)	14.56(41)	0.956(165)
5	324.1(43)	0.0(0)	0.0(0)	33.0(43)	13.84(44)	0.915(163)
6	320.8(47)	0.0(0)	0.0(0)	32,7(47)	12.86(47)	0.877(159)
7	297.3(50)	0.0(0)	0.0(0)	30.3(150)	12.18(51)	0.846(156)
8	245.1(52)	0.0(0)	0.0(0)	25.0(52)	13.09(55)	0.823(152)
9	156.36 5/11	0.06 0)	0.0(0)	15 9(54)	14.97(58)	0.810(150)

THE MAXIMUM TRANSFERRED ENERGY (ENTHRU) WAS 20.9 K-FT

STROKES AMALYZED AND LAST RETURN (FT) 5.2 5.2



RULT= 180.0, AT TOE= 14.4 TONS

TRANSFERRED ENERGY, MAX= 17.8 K-FT
FIN= 13.0 K-FT
TRANSFERRED FNERGY, MAX= 21.7 K-FT
FIN= 16.9 K-FT

	TABLE OF	EXTREME VAL	UES FOR DIL	E AND TIME	OF OCCURRENCE	F
ELFM.	FMAX:	FMIN .	HINSTR	MAYSTR	VELHX	DISMX
Nn.	KTPS	KIPS -	KSI	KST	FT/S	INCH
1	419.3(98)	0.0(0)	0.0(0)	42.7(98)	18.20(30)	0.890(121)
2	408.4(101)	0.0(0)	0.0(0)	41.6(101)	18,03(33)	0.842(122)
3	391.0(69)	0.0(0)	0.0(0)	39,8(69)	17.71(36)	0.787(122
4	390.5(86)	0.0(0)	0.0(0)	39,8(86)	17.09(39)	0.730(124)
5	412.7(83)	0.0(0)	0.0(0)	42.0(83)	15.99(42)	0.671(124
6	413.9(81)	0.0(- 0)	0.0(0)	42.1(81)	14.36(45)	0.616(128
7	365.0(83)	0.0(0)	0.0(0)	37,2(83)	12.75(49)	0.576(135
8	300.2(84)	.0.0(0)	0.0(0)	30.5(84)	12.51(53)	0.548(136
9	181.2(85)	0.0(.0)	0.0(0)	18.4(85)	13.12(56)	0.531(135)

THE MAXIMUM TRANSFERRED ENERGY (ENTHRII) WAS 21.7 K-FT STROKE'S ANALYZED AND LAST RETURN (FT) 5.4 6.3 6.3



RHLT= 240.0, AT TOF= 19.2 TONS

TRANSFERRED FNERGY, MAX= 21.0 K-FT FIN= 13.0 K-FT TRANSFERRED FNERGY, MAX= 23.2 K-FT FIN= 15.3 K-FT

	TAB	LE OF	EXTRE	E VALI	JES FOR	PILE	ר ממא ב	TME	OF OCCURREN	c E
ELEM	· FMAX		FMIN		MINSTE	?	MAXST	rR	VELMX	DISHY
NO.	KIPS		KIPS		KSI		KS1	r	FT/S	INCH
1	515.7(9	6)	0.00	0)	0.00	0)	52.50	96)	20,96(29)	0.839(104
2	499.3(9	3)	0.00	0)	0.00	0)	50.20	93)	20.76(32)	0.761(109
3	486.8(8	9)	0.00	0)	0.00	0)	49.60	89)	20.36(35)	0.687(111
4	491.8(8	5)	0.00	0)	0.00	0)	50.10	85)	19.56(38)	0.616(114
5	510.46 8	1)	0.00	0)	0.00	05	52.00	81)	18.08(41)	0.539(115
6	501.00 7	9)	0.00	0)	0.00	0)	51.00	79)	15.82(44)	0.464(117
7	416.7(7	9)	0.00	0)	0.00	0)	42.40	79)	13.37(48)	0.398(120
8	320.00 8	3)	0.00	0)	0.00	0)	32.60	83)	12.01(51)	0.349(124
9	195.30 5	3)	0.00	0)	0.00	0)	19.90	53)	11.34(54)	0.323(124

THE MAXIMUM TRANSFERRED ENERGY (ENTHRI) WAS 23.2 K=FT
STROKES ANALYZED AND LAST RETURN (FT) 6.9 7.4 7.4



ERICTION PILE

SUMMARY

NO	RHLT	BLOW CT	STROKE	MIN STR	MAX STR	BLOWS/	B.C. PR.	FHFL
	TONS	RPF	FT	KSI	KSI	MINUTE	PSI	RFn.
1	60.0	۶.	3.99	r.00	27.42	58 • 1	N/A	N/A
2	90.0	11.	4.79	0.00	31.24	53+3	N/A	N/A
3	120.0	17.	5.19	0.00	34.06	51.4	N/A	NIA
4	180.0	28.	6.34	0.00	42.69	46.7	N/A	N/A
5	240.0	54.	7.35	0.00	52.52	43.5	N/A	N/A



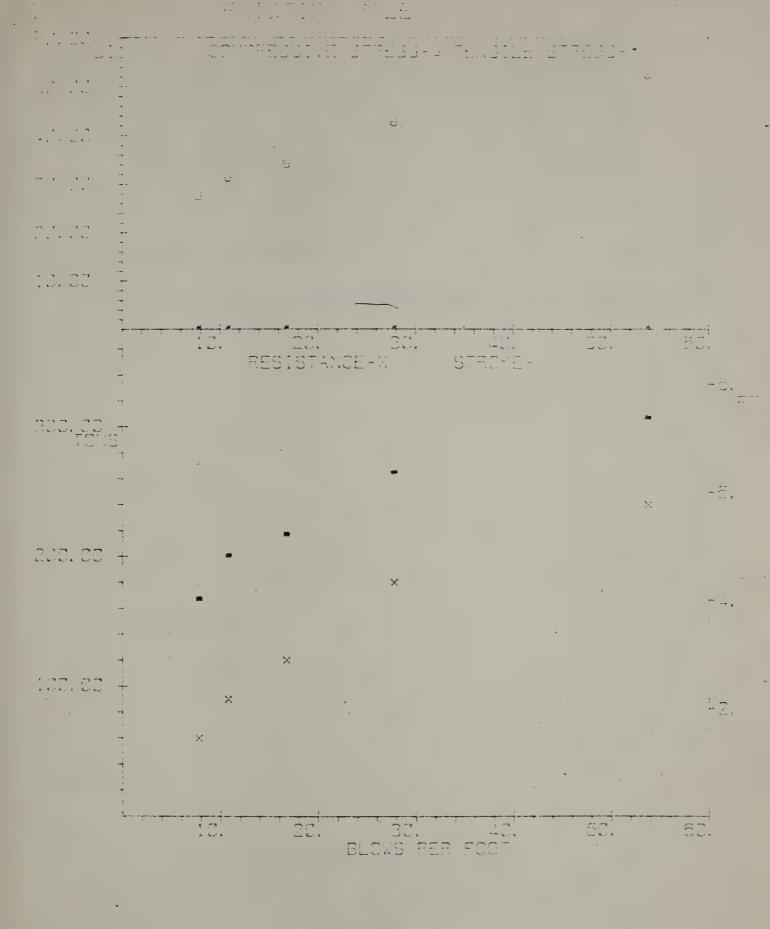
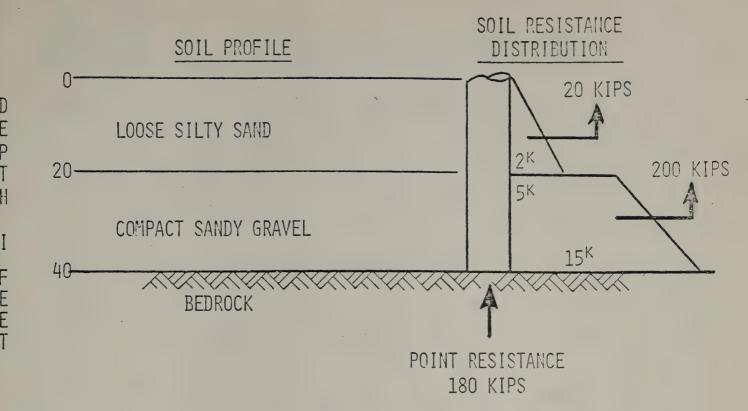


FIGURE 3C-8





PILE DESIGN LO	AD	•	100 TONS
ULTIMATE SOIL	RESISTANCE (SAFETY	FACTOR = 2)	200 TONS
LENGTH FOR 200	TON RESISTANCE		40 FEET
PILE TYPE	- 16 INCH DIAMETER	PIPE,	0.344 INCH WALL
CASE DAMPING V	ALUES		
S	KIN LAYER 1 LAYER 2	US	SE 0.2
To the second	OE		0.1
QUAKE VALUES S	KIN		0.1
Т	OE		0.1

DESIGN DATA FOR WAVE EQUATION ANALYSIS

END BEARING PILE EXAMPLE

FIGURE 4A



INPUT CARD REFERENCE NO.	D	DESIGNATION OF NECESSARY INPUT
	_	TITLE
1.0		END BEARING PILE
	TUCI	IHAMR IPERCS
2.0	10, ,	4, ,,,,,, -92 *
	WT. CAP	STIFF-CB
3.0	1.2,	21,000., *
		C.O.RCB
4.0	,	0.8, *
	LENGTH	AREA-PILE TOP
5.0	40.0,	16.9, *
	QUAKE-SKIN	QUAKE-TOE DAMP-SKIN DAMP-TOE RULT
6.0	0.1,	0.1, 0.2, 0.1, -1.0,*
	X _{PI}	% SOIL RESISTANCE
6.401	0.0	0.0
6.402	20.0	2.0
6.403	20.0	5.0
6.404	40.0	15.0
7.0	BLANK	
8.0	BLANK	
	· ULTI	IMATE RESISTANCE
9.0		50.0, 200.0 250.0 300.0 *
	CASE WA	AVE EQUATION INPUT
		ARING PILE EXAMPLE
		FIGURE 4B



END REARING PILE

PILE DESCRIPTION

X	BEL.	TOP (F	T)	0.0	40.0
Α	(SQ.	IN.)		16.9	16.9
E	(KST)		29000.	29000.
GA	AMMA	(LB/CII	FT)	492.0	492.0

		0	- 3.6
	HAMMER MODI	EF NFF U.	- 22
ELEMENT	WEIGHT	STIFFNESS	COFFF.
NUMBER	(KIPS)	(K/IN)	RESTITUTION
1	1.213		
2	1.213	191666.7	
3	1.213	191666.7	
4	1.213	191666.7	
ANVIL	1.595	101833.3	0.850
CAP	1.200	21000.0	0.800
CUSHION		0.0	1.000
PILE TOP			0.850

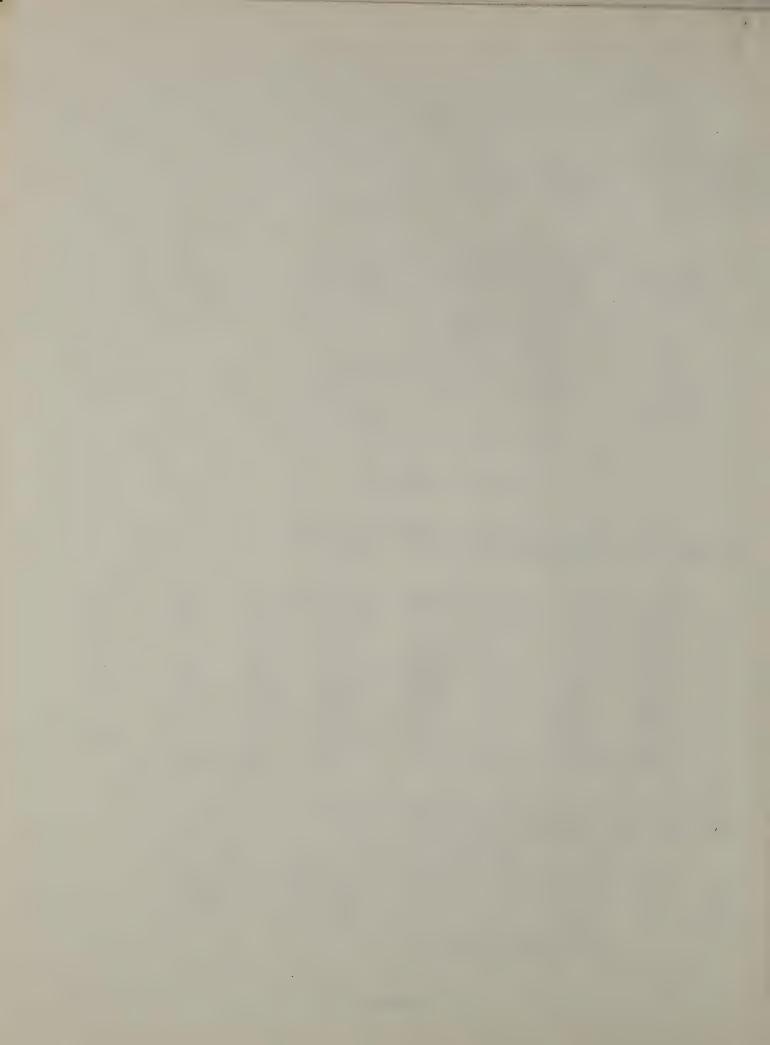
PILE PROPERTIES

PILE LENGTH= 40. FT., AREA(AT TOP)= 16.9 STN
E. MODUL(AT TOP)=29000. KSI., SPEC. WT.(AT TOP)= 492. LRS/CU FT

	WEIGHT	STIFFN.	PDAMP.	SPLICE	SOIL-S	snIL-n	QUAKE	L.B.T.
NO.	(KIPS)	(K/IN)	(KS/FT)	(KIPS)	(PCT.)	(KS/FT)	CIN.)	(FT.)
1	0.257	9189.	0.59	. 0.	0.011	0.073	0.100	4.4
2	0.257	9189.	0.59	- 5000.	0.034	0.220	0.100	8.9
3	0.257	9189.	0.59	-5000.	0.057	0.366	0.100	13.3
4	0.257	9189.	0.59	~ 5000.	0.080	0.513	0.100	17.8
5	0.257	9189.	0.59	= 5000.	0.102	0.659	0.100	22.2
6	0.257	9189.	0.59	- 5000•	0.125	0.806	0.100	26.7
7	0.257	9189.	0.59	-5000.	0.148	0.952	0.100	31.1
8	0.257	9189.	0.59	=5000.	0.170	1.098	0 - 100	35.6
9	0.257	9189.	0.59	-5000.	0.193	1.245	0.100	40.0
TOE					0.080	2.966	0.100	

COEFFICIENT OF RESTITUTION OF SOIL 1.000 SKIN FRICTION CONSTANT FOR ALL RULT VALUES

		OPTIONS AND	SPECIFICAT	Inns	
PHI	1.40	S-DAMPING	VISCOUS	RWT (KIPS)	0.00
IOUT	10	P-DAMPING	1	SOIL DIST. NO.	0
IFUEL	1	J SKIN	0.20	TOEL (SEC.)	0.0000
INSTR	0	J TOE	0.10	TEMAX (MS)	0.00
		TIME THEP	(MS)0.091		



RULT= 120.0, AT TOE= 9.6 TONS

TRANSFERRED FNERGY, MAX= 17.5 K=FT FIN= 15.9 K=FT TRANSFERRED ENERGY, MAX= 20.6 K=FT FIN= 19.1 K=FT

	ТА	BLE	OF EXTRE	EME 1	VALUES FO	IR PI	LE AND	TIME	of necul	RRENO	E
ELEM	· FMAX		FMI	1	MINS.	TR	MAXS.	TR	VELM	<	DISMX
No.	KTPS		KIP:	5	KS	Ţ	KS:	1	FT/	5	INCH
1	507.50	30)	0.00	0)	0.00	0)	30.00	30)	15.09(31)	0.897(166)
2	512.00	33)	0.00	0)	0.00	0)	30.30	33)	14.87(34)	0.876(171)
3	511.00	36)	0.00	0)	0.00	(0)	30.20	36)	14.53(37)	0.857(178)
4	504.00	39)	0.00	0)	0.00	0.)	23°8(39)	14.08(40)	0.840(178)
5	491.4(42)	0.00	0)	0.00	0)	29.1(42)	13.510	43)	0.824(178)
6	473.3(45)	0.00	0)	0.00	0)	28.00	45)	12.87(46)	0.808(180)
7	443.60	48)	-4.4(66)	-0.3(66)	26.20	48)	12.79(50)	0.795(190)
8	375.20	51)	- 35.3(65)	-2.10	65)	22.20	51)	15.08(55)	0.791(1891
9	245.8(52)	-28.9(64)	-1.7(64)	14.50	52)	18.34(57)	0.788(189)

THE MAXIMUM TRANSFERRED ENERGY (EMTHRU) WAS 20.6 K-FT

STROKES ANALYZED AND LAST RETURN (FT) 5.0 5.7 5.5



RULT= 160.0, AT TOE= 49.6 TONS

TRANSFERRED FNERGY, MAX= 22.0 K=FT
FIN= 18.9 K=FT
TRANSFERRED FNERGY, MAX= 21.1 K=FT
FIN= 18.0 K=FT

	T	ABLE	OF EXTRE	uE V	ALUES FOR	PI	LE AND T	IME	OF OCCURRENC	Ε
ELEM		X	FMIN		MINSTR	?	MAXST	rR	VELMX	DISMX
NO.	KIP	5	KIPS		KSI		KS1		FT/S	INCH
1	557.10	29)	0.00	0)	0.00	0)	33.00	29)	16.90(30)	0.772(132)
2	561.90	32)	0.00	0)	0.00	0)	33.20	32)	16.64(33)	0.741(133)
3	560.60	35)	0.00	0)	0.00	0)	33.20	35)	16.24(36)	0.709(130)
4	553.11	38)	0.00	0)	0.00	0)	32.7(38)	15.73(40)	0.678(129)
5	540.71	42)	0.00	0)	0.00	0)	32.00	42)	15.11(43)	0.648(146)
6	524.40	45)	0.00	0)	0.00	0)	31.00	45)	14.41(46)	0.625(145)
7	496.5(48)	0.00	0)	0.00	0)	29.4(48)	14.07(49)	0.602(142)
8	435.30	50)	0.00	0)	0.00	0)	25.80	50)	15.45(53)	0.583(141)
9	318.50	52)	0.00	0)	0.00	0)	18.8(52)	18,48(57)	0.567(146)

THE MAXIMUM TRANSFERRED ENERGY (ENTHRII) WAS 21.1 K-FT STROKES ANALYZED AND LAST RETURN (FT) 6.8 6.2 6.2

RILT= 200.0, AT THE= 89.6 THMS

TRANSFERRED ENERGY, MAX= 19.2 K=FT FIN= 15.3 K=FT

	TABLE OF	EXTREME VA	LUES FOR PIL	E AND TIME	OF OCCURRENC	E
ELEM	· FMAX	FMIN	MINSTR	MAXSTR	VELMX	DISMX
NO.	KIPS	KTPS	KSI	KSI	FT/S	INCH
1	555.8(29)	0.0(0)	0.0(0)	32.9(29)	16.72(30)	0.655(119)
2	560.8(32)	0.0(0)	0.0(0)	33.2(32)	16.45(33).	0.621(118)
	559.7(35)	0.0(0)	0.0(0)	33.1(35)	16.05(36)	
4	552,5(38)	0.0())	0.0(0)	32.7(38)	15.53(40)	0.552(114)
	540.7(42)	0.0(0)	0.0(0)		14.91(43)	
	524.6(45)	0.0(0)	0.0(0)		14.19(46)	
	498.1(48)	0.0(0)	0.0(0)		13.72(49)	0.458(105
	444.2(50)	0.0(0)	0.0(0)		14.26(53)	
9	358.4(53)	0.0(0)	0.0(0)	21.2(53)	15.93(57)	0.410(103)

THE MAXIMUM TRANSFERRED ENERGY (ENTHRII) WAS 19.2 K*FT STROKES ANALYZED AND LAST RETURN (FT) 6.4 6.6

